

## SIMULATION AND IDENTIFICATIONS OF ALTERNATOR TRANSFER FUNCTIONS

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**Abstract:** In this paper, a procedure for identifying the transfer functions of Park's dq-axis model of a synchronous generator has been developed for analyzing automotive charging systems. This application note focuses on one particular aspect of charging system design: alternator/regulator performance. Two of these transients, a load-dump condition (heavy electrical load switching with a disconnected battery), and an engine rapid crankshaft speed-up, are examined. aximum 200 words.

**Key words:** Transfer functions, synchronous generator, automotive.

### 1. INTRODUCTION

Recent advances in power electronics applied to alternators. Constant speed operation has not been the choice of alternators designers, but rather a necessity brought about by the fixed relationship between the speed of the DC generators and the fixed utility grid frequency. The two main advantages of variable speed operation over constant speed operation are additional energy capture at partial load and potential reduction of fatigue loads.

The design of such a robust frequency converter controller for high dynamic performance requires that the synchronous generator model parameters are known accurately. In principle, synchronous machine parameters may be determined either from design calculations or from measurements acquired at the factory or on site. Many papers have been published on synchronous machine parameter identification [1–6]. Most papers address standstill frequency response (SSFR) methods following the protocols of IEEE Standard 115-1995 [7]. This standard focuses on identifying equivalent circuit parameters rather than on transfer functions. A few papers address methods of identifying the parameters from time-domain data. In both cases, the parameter estimation process generally consists of two parts. First, the time constants are extracted by applying a curve-fitting procedure to measured data. Next, the equivalent circuit parameters are determined by solving a set of nonlinear equations through numerical optimization. In this paper, a procedure is developed [5] for identifying the transfer functions of Park's dq-axis model of a synchronous generator from time-domain standstill step-response data.

### 2. MODELING THE ALTERNATOR

The aim of this section is to set up a theoretical model of alternator operating like synchronous generator suited for both time-domain simulation and model based control design. In essence, there are two aspects that need to be modeled: the mechanical and the electromagnetic part. The mechanical part can be modeled using the techniques outlined in Molenaar [9]. In the present paper, we will restrict to the dynamic modeling of the electromagnetic part. From a modeling point of view, all synchronous generators have similar representations. They differ

only with respect to some model parameters. Because the round-rotor synchronous generator is a special case of the salient-pole rotor synchronous generator, we will treat only the latter for an arbitrary number of pole-pairs  $p$ . Damper windings are real or fictitious windings that can be used to represent, for example, the damping effects of eddy currents in the machine. In Fig. 1, one damper winding is located along the direct-axis, and one along the quadrature-axis (represented by  $R_{1d}$  and  $R_{1q}$  in Fig. 1).

According to Park [10,11], the voltage equations of an ideal synchronous generator, linear magnetic circuit and stator windings are sinusoidal distributed along the stator circumference in the  $dq$  reference frame are given by (using generator sign convention for the stator circuits):

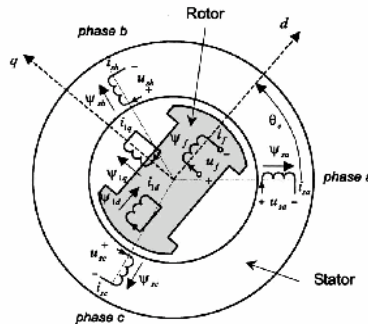
$$\begin{aligned} u_d &= -R_s i_d - \omega_e \psi_q - \frac{d}{dt} \psi_d \\ u_q &= -R_s i_q + \omega_e \psi_d - \frac{d}{dt} \psi_q \\ -u_f &= -R_f i_f - \frac{d}{dt} \psi_f \end{aligned} \tag{1}$$

with  $u_d$  the direct-axis voltage [V],  $R_s$  the stator-winding resistance [S],  $i_d$  the direct-axis current [A],  $T_e = d\theta_e / dt$  the electrical angular frequency [rad/s],  $R_q$  the quadrature-axis winding flux [ $V_s$ ],  $t$  time [s],  $R_d$  the direct-axis winding flux [ $V_s$ ],  $u_q$  the quadrature-axis voltage [V],  $i_q$  the quadrature-axis current [A],  $u_f$  the field-winding voltage [V],  $R_f$  the field-winding resistance [S],  $i_f$  the field-winding current [A], and  $R_f$  the field-winding flux [ $V_s$ ].

A few observations can be made. The most important one is that (1) are coupled via the fluxes. In addition, they depend on the electrical angular frequency  $T_e$ , thereby introducing non-linearity's. The fluxes are given by

$$\begin{aligned} \psi_d(s) &= L_{do}(s)I_d(s) + L_{dfo}(s)I_f(s) \\ \psi_q(s) &= L_q(s)I_q(s) \\ \psi_f(s) &= L_{fdo}(s)I_d(s) + L_{fo}(s)I_f(s) \end{aligned} \tag{2}$$

with  $s$  the Laplace operator,  $R_{d,q,f}$  the Laplace transformed fluxes,  $I_{d,q,f}$  the Laplace transformed currents, and  $L_{do}(s)$ ,  $L_{fdo}(s) = L_{dfo}(s)$ ,  $L_q(s)$ ,  $L_{fo}(s)$  proper transfer functions.  $L(s)$  when  $s$  is infinite is a finite zero (or non-zero constant) which depend on the design of the generator.



**Figure 1 – Schematic representation of an elementary three-phase, synchronous generator.**

For a finite number of damper windings, the aforementioned transfer functions can be expressed as a ratio of polynomials in  $s$  [12]. Furthermore, in his original paper R. H. Park used the non-power in-

variant transformation to transform the stator quantities onto the  $dq$  reference frame that is fixed to the rotor.

The dynamic behavior of an ideal synchronous generator is thus fully described by the sets (1) and (2) expressed in the  $dq$  reference frame. For time-domain simulation purposes, it is convenient to rewrite the first set of equations in the following form

$$\begin{aligned} \psi_d &= -\int (u_d + R_s i_d + \omega_e \psi_q) dt \\ \psi_q &= -\int (u_q + R_s i_q - \omega_e \psi_d) dt \\ \psi_f &= \int (u_f - R_f i_f) dt \end{aligned} \quad (3)$$

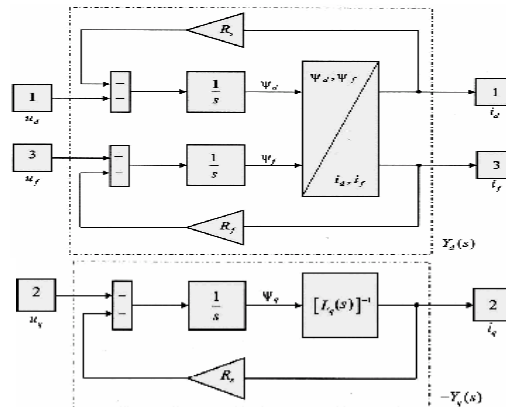
with the fluxes as state variables. The rotor flux equations can be conveniently expressed in matrix form

$$\begin{bmatrix} \psi_d \\ \psi_f \end{bmatrix} = \begin{bmatrix} L_{do}(s) & L_{fdo}(s) \\ L_{fdo}(s) & L_{fo}(s) \end{bmatrix} \begin{bmatrix} I_d \\ I_f \end{bmatrix} \quad (4)$$

It can be easily shown that the inverse transformation is given by

$$\begin{bmatrix} I_d \\ I_f \end{bmatrix} = \frac{\begin{bmatrix} L_{fo}(s) & -L_{fdo}(s) \\ -L_{fdo}(s) & L_{do}(s) \end{bmatrix}}{L_{do}(s)L_{fo}(s) - L_{fdo}^2(s)} \begin{bmatrix} \psi_d \\ \psi_f \end{bmatrix} \quad (5)$$

From those equations, we can conclude blocks diagrams



**Figure 2 – Block diagram of an ideal synchronous machine.**

In addition, it can be shown that the denominators of  $L_{do}(s), L_{fdo}(s), L_{fdo}(s), L_{fo}(s)$  are identical. Consequently, the denominators in the above matrix equation are identical. For simulation as well as control design purposes, accurate information about the transfer functions  $L_{do}(s), L_{fdo}(s), L_{fo}(s)$ , and  $L_{fo}(s)$ , as well as the resistances  $R_s$  and  $R_f$ , is required.

### 3. IDENTIFICATION OF PARAMETERS

Synchronous machine identification and parameter determination can be performed either during normal operation (on-line), or during specially designed identification experiments (off-line).

#### A. Quadrature-Axis Identification

Synchronous machine identification and parameter determination can be performed either during normal operation (on-line), or during specially designed identification experiments (off-line).

The dynamic behavior of the quadrature-axis of an ideal synchronous generator is fully described by the transfer function  $Y_q(s)$  in Fig. 2. From the block diagram it directly follows that

$$Y_q(s) = -\frac{I_q(s)}{U_q(s)} = \frac{1}{R_s + sL_q(s)} \quad (6)$$

For the identification of  $Y_q(s)$ , knowledge of the quadrature-axis voltage  $u_q(t)$  and current  $i_q(t)$  is thus both necessary and sufficient. An appropriate rotor position for quadrature-axis identification is the one when the field winding axis is parallel to the  $a$ -phase winding (i.e.,  $2_e = 0$ , see Fig. 1). In addition, if in this position the stator  $b - c$  terminals are excited while the  $a$ -terminal remains open  $i_a(t)=0$ , it follows that  $i_b(t) = -i_c(t)$ . It can be concluded that  $u_d(t)=1/2(u_b(t)+u_c(t))$ .

Substituting the above results in the equations for the transformed stator voltages and currents

$$\mathbf{u}_{0dq} = T_{0dq} \mathbf{u}_s \quad \mathbf{i}_{0dq} = T_{0dq} \mathbf{i}_s$$

where

$$\mathbf{u}_{0dq} = \begin{bmatrix} u_0 & u_d & u_q \end{bmatrix}^T$$

$$\mathbf{u}_s = \begin{bmatrix} u_a & u_b & u_c \end{bmatrix}^T$$

$$\mathbf{i}_{0dq} = \begin{bmatrix} i_0 & i_d & i_q \end{bmatrix}^T$$

and  $T_{0dq}$  the Park's power-invariant transformation matrix,

$$T_{0dq} = \sqrt{\frac{2}{3}} \begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \cos(\theta_e) & \cos(\theta_e - \frac{2}{3}\pi) & \cos(\theta_e + \frac{2}{3}\pi) \\ \sin(\theta_e) & \sin(\theta_e - \frac{2}{3}\pi) & \sin(\theta_e + \frac{2}{3}\pi) \end{bmatrix}$$

gives

$$\begin{aligned} u_q &= \frac{1}{2}\sqrt{2}(u_c - u_b) & u_d &= 0 \\ i_q &= \sqrt{2}i_c & i_d &= 0 \end{aligned} \quad (7)$$

Finally, the q-axis parameters ( $L_q(s)$  and  $R_s$ ) are deduced algebraically from the transfer function  $Y_q(s)$ .

## B. Quadrature-Axis Identification

The dynamic behavior of the direct-axis of an ideal synchronous generator is fully described by the transfer function matrix  $Y_d(s)$  between  $u_d, u_f$  and  $i_d$ , if in Fig. 2. In this case, rotor position is the one when the field winding axis is perpendicular to the  $a$ -phase winding (i.e.,  $2_e = \pi/2$ , see Fig. 1). After all, it can be easily shown that for  $2_e = \pi/2$  it follows that:

$$\begin{aligned} u_d &= \frac{1}{2}\sqrt{2}(u_c - u_b) & u_q &= 0 \\ i_d &= \sqrt{2}i_c & i_q &= 0 \end{aligned} \quad (8)$$

In principle, the elements of (5)  $L_{fd}(s), L_{fdo}(s)$ , and  $L_{do}(s)$  can be identified using data acquired from two independent measurements, namely one with excitation of the quadrature-axis voltage while the field winding is left open and one when the field winding is short-circuited [13]. Combining the resulting transfer functions gives the required 2x2 transfer function matrix.

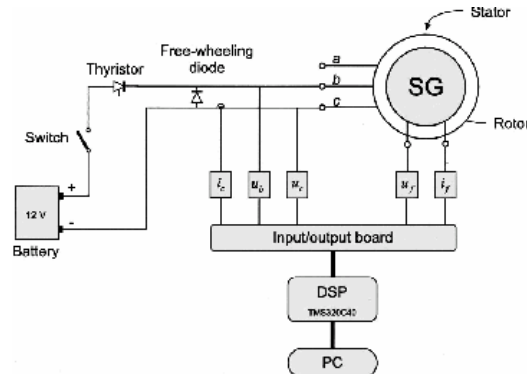
One way to overcome this problem is to identify the transfer function between the fluxes  $\mathcal{R}_d, \mathcal{R}_f$  and the currents  $i_d, i_f$  and assuming that both  $R_s$  and  $R_f$  are known. Recall that

the stator winding resistance is known from the quadrature-axis identification. One possible way to determine the field winding resistance is by a stepwise excitation of  $u_f$  and measuring  $i_f$ .

Neither the direct-axis winding flux  $R_d$ , or the field winding flux  $R_f$ , however, can be measured in practice. Conversely, these variables can be generated by integration of (3) with the  $u_d$ ,  $u_f$ ,  $i_d$ , and  $i_f$  acting as input. Analogous to the quadrature-axis identification, the latter variables can be deduced from the three measurable variables  $u_b$ ,  $u_c$ , and  $i_c$ .

#### 4. MEASUREMENT SET-UP

This model includes all of the internal flux coupling factors that vary with the shaft rotation angle.



**Figure 3 – Scheme of the measurement set-up of the modified step-response test as used for the identification of the machine parameters.**

Figure 3 shows a schematic of the measurement set-up. The step-like excitation signal is generated by switching on a low-power DC voltage source (i.e., a 12V battery). The battery is connected to the b and c stator terminals of the alternator.

Depending on the measurement type, a combination of the following signals is measured:  $i_c$ , (stator current),  $u_{bc}$  (stator voltage),  $u_f$  (field winding voltage), and  $i_f$  (field winding current).

The data-acquisition system consists of three main parts, an input-output I/O board, a digital signal processor board from with a TMS320C40 processor from Texas Instruments®, and a personal computer (PC) connected to the processor board.

#### A. Data-Acquisition and Identification Procedure

The modified step-response test consists of three successive measurements:

1. Q-measurement. Rotor positioned such that the quadrature axis is excited;
2. D-measurement. Rotor positioned such that the direct axis is excited, while the field winding is short-circuited;
3.  $R_f$ -measurement. Stepwise excitation of  $u_f$  and measuring  $i_f$ .

#### B. Parameter Estimation Procedure

System identification or parameter estimation deals with constructing mathematical models of dynamical systems from experimental data. In this method, the parameters of the model are chosen so that the difference between the model output and the measured output is minimized.

The developed identification procedure consists of next steps:

**Model structure and order selection.** The measured input-output data is imported into graphical user interface. If the resulting model, however, produces an unsatisfactory simulation error and/or if the input is correlated with the residual, the model is rejected and another model structure (or order) is selected. This continues until the model produces a satisfactory simulation error and results in zero cross-covariance between residual and past inputs. In that case it can be concluded that a consistent model estimate has been obtained;

**Model validation.** Model validation is highly important when applying system identification. The parameter estimation procedure picks out the best model within the chosen model structure. The

crucial question is whether this *best* model is *good enough* for the intended application: time-domain simulation, analysis of dynamic loads, or control design purposes.

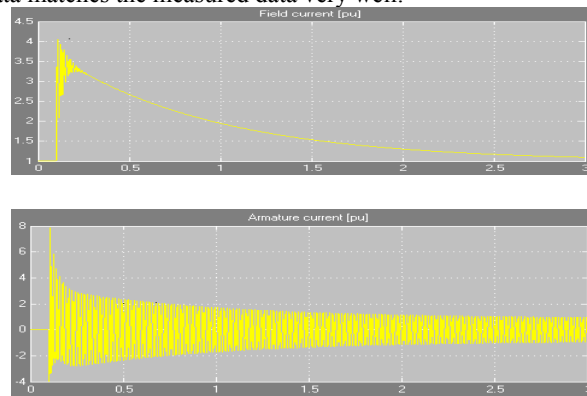
### C. Model Validation

As mentioned above, the outputs of the identified model are compared to the measured ones from a validation data set to (in)validate the model. The percentage of the output variations that is reproduced by the model is chosen as measure of the goodness of fit.

### D. Results

The q-axis transfer function  $Y_q(s)$  of the electromagnetic part of the generator has been identified. A third order model turns out to be sufficient. The q-axis parameters are derived from  $Y_q(s)$  as outlined above.

The resulting inputs and outputs of the model are shown in Fig. 4 for a validation data set. Obviously, the simulated data matches the measured data very well.



**Figure 4 – Scheme of the measurement set-up of the modified step-response test as used for the identification of the machine parameters.**

Observe that it is not equal to zero because the short-circuit is not perfect due to the slip-rings.

## 5. CONCLUSIONS

In this paper, a procedure for identifying the transfer functions of Park's dq-axis model of a synchronous generator has been developed. The following conclusions can be drawn:

- A theoretical model of the electromagnetic part of a synchronous generator has been proposed. It has been shown that the parameters of this model can be easily identified following the developed procedure.
- The validity of the theoretical model has been verified by comparing time-domain simulations with measurements.

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